AN ON-LINE OPTIMAL ARTIFICIAL NEURAL NETWORK-BASED CONTROLLER FOR SIMPLIFIED ORDER POWER SYSTEMS

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The paper presents an on-line optimal artificial neural network (ANN)- based controller for simplified order power systems to improve the dynamic response under different operating conditions. The original $13^{\text{th}}$ order power system is reduced to $5^{\text{th}}$ order model. The basic feature of the proposed ANN controller is that it consists of two neural networks, one of them (ANN1) maps the optimal control process at different loading conditions and the other (ANN2) maps the feedback control to produce the required control action signal. The ANN1 is trained using input/output pairs of data which are collected from the optimal control of the reduced order model of power system at different loading conditions The ANN2 parameters are adapted on-line through the ANN1 according to loading conditions. The digital simulation results proved the high performance of the synchronous generator using the proposed ANN controller in terms of fast response and less undershot/overshot under different operating conditions. A comparison between the off-line fixed parameters optimal controller and the proposed ANN controller validates the effectiveness and reliability of the ANN controller.

**KEYWORD:** Reduction Technique, power systems, optimal controller, ANN controller.

**NOMENCLATURE**

$q$-axis reactance $x_q$
d-axis reactance $x_d$
$q$-axis mutual reactance $x_{mq}$
d-axis mutual reactance $x_{md}$
$q$-axis damper winding reactance $x_{kq}$
d-axis damper winding reactance $x_{kd}$
Field winding reactance $x_{fd}$
Transmission lines reactance $x_l$
Transmission lines resistance $r_l$
Inertia constant $M$
Steady state speed governor regulation $R_g$
Governor time constant $T_g$
1. INTRODUCTION

Power systems are continuously increasing in size in national and international levels. Inter-connected unified networks are installed in nearly all countries and continent. Consumers demand of electricity increases day after day all over the world. Stable operation of such large power systems is a necessity for all people. Power systems are usually subjected to continual impacts due to lines and loads switching and different types of faults due to malfunctions of utility drives or failures at consumer's networks or loads. According to these interconnections, the systems orders become relatively high and the complexity is increased. Therefore, the analysis of dynamic stability and controller's design of these large interconnected power systems becomes time consuming and laborious in order to have an accordance order representation of high-order power systems, model reduction techniques are used for getting simplified models with adequate accordance. Several methods for model reduction are based on eigenvalue analysis of the system linearized differential equations [1,2]. Davison [1] had used the eigenvalues and eigenvectors of the complete system model to compute a reduced model of smaller order than the original. In this method, the dominant eigenvalues are to be chosen with real parts closest to the imaginary axis.

Transient stability is of main concern to power systems engineers, as its loss can lead to dangerous electromechanical oscillations or to partial or complete blackouts. Damage of synchronous generators shafts can also occur. Preservation of such transient stability is assured by the presence of capable and effective controls. An additional signal to the excitation and/or mechanical system is currently being used for improving the damping characteristic of the synchronous generator under disturbance conditions. The classical controllers with filters fed from speed signals are well known and used in practice [3]. Modern optimal control theory has now been used in this field [4, 5]. Normally, the parameters of optimal controller are designed at certain operating point to give a good performance. However, the system dynamic response may deteriorate when operating point changes.

The artificial intelligent neural network (ANN) has been developed for improving systems dynamic performance and to adapt controller parameters in real time due to any change in the loading conditions [6-12]. Dejan J. S. and Y. H. Pao, in 1989 used an ANN based to evaluate the critical clearing time of the power system [6]. An ANN based power system stabilizer (PSS) using an on-line measurements of the generator active output power and power factor as an input signals to the PSS is designed by Y.
Y. Hsu and C. R. Chen in 1991 [7]. Y. Zhang, et al have presented an ANN based PSS. They concluded that PSS can provide good damping of the power system over a wide range of operating point and significantly improve the dynamic performance of the system [8]. ANN power system stabilizer based a pole placement state feedback gain as off-line training is presented be El-Sherbiny, et al [9]. They indicate the effectiveness of the proposed ANN controller in comparison with the conventional PI controller. An enhanced adaptive neural network control scheme, based on the adaptive linear element is designed by L. C. Min and L. Qing [10]. This scheme is applied to multi-machine system and it has effectiveness for different types of faults and for a wide range of operating point.

The present paper introduces an optimal ANN controller based on reduced order model of power system. This controller is constructed from two neural networks, one of them (ANN1) maps the optimal control process at different loading conditions and the other (ANN2) maps the feedback control to produce the required control action signal. The ANN2 parameters are adapted on-line through the ANN1 according to loading conditions and the reduction technique is used through the designing stage of such controller in order to retain only the states which are usually observable. The ANN1 is trained using input/output pairs of data which are collected from the optimal control of the reduced order model of power system at different loading conditions.

2. POWER SYSTEM MODEL

The studied power system consists of a 13th order model of a synchronous machine connected to an infinite bus through a transmission line as shown in Fig.1. This model contains of 5th order for winding representation of synchronous machine, 4th order for automatic voltage regulator (AVR)& exciter and 4th order for turbine & governor.

The matrix form for the power system model

\[ \frac{dx}{dt} = Ax + Bu \]  \hspace{1cm} (1)

\[ A_1 x + \frac{1}{\omega_b} A_2 x = Bu \]  \hspace{1cm} (2)

From the above equations the A matrix can be written as

\[ A = -\omega_b A_2^{-1} A_1 \]  \hspace{1cm} (3)

Elements of A-matrix are defined in appendix[a] where

\[ x = [\Delta i_q \ \Delta i_d \ \Delta i_{kq} \ \Delta i_{kd} \ \Delta i_f \ \Delta \delta \ \Delta \omega \ \Delta E_{fd} \ \Delta V_a \ \Delta V_r \ \Delta V_s \ \Delta P_m \ \Delta P_g ]^T \]

\[ u = [\Delta P_L \ \Delta V_c \ \Delta P_c ]^T \]
\[
\begin{array}{c}
\begin{bmatrix}
-v_a & v_d & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
-v_b & v_e & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
-v_c & v_f & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
\end{bmatrix}
\end{array}
\]

\(A_1 = \)

\[
\begin{bmatrix}
-s_x & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & -s_x & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & -s_x & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & -s_x & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & -s_x & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & -s_x & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & -s_x & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & -s_x & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -s_x & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -s_x \\
\end{bmatrix}
\]

\(A_2 = \)

\[
\begin{bmatrix}
-s_x & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & -s_x & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & -s_x & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & -s_x & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & -s_x & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & -s_x & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & -s_x & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & -s_x & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -s_x & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -s_x \\
\end{bmatrix}
\]

\[
B = \begin{bmatrix}
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
\end{bmatrix}
\]

\(T_a = \)

\[
\begin{bmatrix}
K_a & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & K_a & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & K_a & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & K_a & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & K_a & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & K_a & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & K_a & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & K_a & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & K_a & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & K_a \\
\end{bmatrix}
\]

\(T_b = \)

\[
\begin{bmatrix}
K_b & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & K_b & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & K_b & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & K_b & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & K_b & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & K_b & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & K_b & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & K_b & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & K_b & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & K_b \\
\end{bmatrix}
\]

\(T_c = \)

\[
\begin{bmatrix}
K_c & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & K_c & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & K_c & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & K_c & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & K_c & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & K_c & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & K_c & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & K_c & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & K_c & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & K_c \\
\end{bmatrix}
\]
3. REDUCTION TECHNIQUE

The methods of reducing dynamic system are discussed in [3:6]. The differences between these methods are the way of choosing the dominant eigenvalues. The input-output performance indices in [4,5] are used for giving good accuracies. Instead of choosing the eigenvalues closest to the Jw-axis, the eigenvalues which have highest input-output indices can be selected. After the dominant eigenvalues are chosen, the Davision method [3] is used for giving the reduced order model of power system. The model reduction technique is used for reducing a 13th order model for generating unit to 5th order model which is used for controller design. The retained states considered are the rotor angle, the rotor frequency, the exciter voltage and stator current components which are measured for achieving control action.

The A matrix of the system which is given by Eq.(1) can be rewritten as follows:

\[ A = M \Lambda M^{-1} \]  

where:
- \( M \) is the matrix of eigenvectors
- \( \Lambda \) is the diagonal matrix of eigenvalues

The reduced system model is described by following equation

\[ x_r = A_r x_r + B_r u \]  

where

\[ A_r = M_r \Lambda_r M_r^{-1} \]  
\[ B_r = M_r [M^{-1} B] \]

\( A_r \) & \( B_r \) are reduced order constant system matrices.
\( x_r \) is the retained states vector
\( M_r \) is a matrix representing a subset of the complete eigenvector matrix \( M \). The rows of this matrix are selected from \( M \) based on retained states, the columns of \( M_r \) are selected from \( M \) based on retained eigenvalues
\( \Lambda_r \) is a diagonal matrix of retained eigenvalues.

\[
\begin{bmatrix}
M^{-1}B\end{bmatrix}^T
\]
is a diagonal matrix consisting of the retained rows of \( M^{-1}B \) corresponding to \( x_r \).

4. THE OPTIMAL CONTROLLER DESIGN PROCEDURE

The object of the optimal control design is determining the optimal control law \( u(t,x) \) which can transfer system from its initial state to the final state such that a given quadratic performance index is minimized. Considering the reduced order model of power system which is described by Eq. (5). The quadratic performance index \( J \) is described by:

\[
J = \int_{0}^{\infty} (x_r^T Q x_r + u^T R u) \ dt \quad (8)
\]

the optimal control law is written as

\[
u(t) = K_r x_r(t) \quad (9)
\]

where: \( Q \) is positive semi definite matrix and \( R \) is real symmetrical matrix. The problem is to find the vector \( K_r \) of control law. The problem then is to choose \( K_r \) to minimize the performance index \( J \). This problem is discussed in Ref [4] and the \( K_r \) is given by:

\[
K_r = - R^{-1} B_r^T P \quad (10)
\]

The matrix \( P \) is positive definite, symmetric solution to the matrix Ricciti equation which is written as:

\[
P A_r + A_r^T P + Q - P B_r R^{-1} B_r^T P = 0 \quad (11)
\]

Normally the parameters of optimal controller are designed at nominal operating point to give a good performance.

5. OPTIMAL ARTIFICIAL NEURAL NETWORK

Optimal ANN controller based on reduced order model of power system is introduced. This controller is constructed from two neural networks as shown in Fig. 3, one of them (ANN1) maps the optimal control process at different loading conditions and the other (ANN2) maps the feedback control \( u(t) = k x(t) \) to produce the control signal. The ANN2 parameter adapts online through the ANN1 according to loading conditions and the reduction technique is used through the designing stage of such controller in order to retain only the states which are measured (observable states), reduce the consuming time and reduce the neurons which are required for controller structure. The first ANN1 is trained using the input output pairs of data which are collected from the optimal control of the reduced order model of power.
system at different loading condition. The ANN1 have 2 input nodes [P, Q] and 4-nodes in hidden layer and also 5-nodes in the output layer. The output of the ANN1 is the weights of ANN2. The ANN2 contains the 5 nodes in input layer [the five interesting states] and one node in output layer [control signal]

5.1 The Operation Steps of a ANN1

Step 1: Nodes of the input layer receive signals from the loading condition, the input vector is \( Pq \)

\[ Pq = [P; Q] \]  

(12)

Step 2: Output of the input layer passes to hidden nodes through the weighted links, the resulting weight matrix between the hidden and input neurons is given by \( w_{11} \) and the hidden nodes biases are given by the \( b_{11} \).

Step 3: The output of hidden nodes results from input signal passing through the activation function (tan sigmoid transfer function), the hidden layer output vector of ANN1 is \( oh \), where

\[ oh = \text{tansig}(w_{11} * Pq, b_{11}) \]  

(13)

Step 4: Hidden layer outputs sent to the output nodes through weighted links, the resulting weight matrix between the hidden and output neurons is given by \( w_{21} \) and the hidden nodes biases given by the \( b_{21} \).

Step 5: The ANN1 output is obtained using another activation function (Linear transfer function), the output vector of ANN1 is \( o_1 \), where

\[ o_1 = \text{purelin} (w_{21} * oh, b_{21}) \]  

(14)

5.2 The Operation Steps of a ANN2

The following steps describe the operation of a ANN2

Step 1: Nodes of the input layer receive signals from the outside world, the input vector is \( Xr \)

\[ Xr = [\Delta \delta; \Delta \omega; \Delta E_{fd}; \Delta i_q; \Delta i_d] \]  

(15)

Step 2: Output of the input layer passes to output node through the weighted links, the weight matrix between the input and output neuron is given by \( w_2 \).

\[ w_2 = o_1 \]  

(16)

\( o_1 \) is the output vector of ANN1 is described by equations (12:14).

Step 3: The ANN1 output is obtained using activation function (Linear transfer function), the output of ANN2 is control signal \( (u) \)

\[ u = \text{purelin} (w_2 * Xr, b_2) \]  

(17)

The equations from 12 to 17 describe the operation of the proposed artificial neural network controller. The ability of this controller to adapt its parameters with itself dependS on the loading conditions. The closed loop matrix of system with ANN can be calculated as:

\[ A_{ANN} = A_r - B_t * w_2 \]  

(18)
6. DIGITAL SIMULATION RESULT

The power system shown in Fig. 1 is used for digital simulation. It consists of a synchronous machine connected to an infinite bus through a transmission line. The complete data of this system are given in appendix (b). The model reduction technique is given in [2], which is used for reducing the 13<sup>th</sup> order model of generating unit (A,B in Eqn.1) to 5<sup>th</sup> order model (A, ,B<sub>r</sub> in Eqn.5). At nominal operating point P=.75, Q=0.0 and the reduced order models is calculated as follows:
Table 1 gives the eigenvalues of both the original and reduced order models and the corresponding time response is dedicated in Fig. 4.

**Table 1 : The eigenvalues of the original and reduced power system models.**

<table>
<thead>
<tr>
<th>Eigenvalues of 13(^{th}) order model</th>
<th>Eigenvalues of 5(^{th}) order model</th>
</tr>
</thead>
<tbody>
<tr>
<td>-1000</td>
<td>-3.5219 + 15.2508i</td>
</tr>
<tr>
<td>-26.935 + 376.49i</td>
<td>-3.5219 - 15.2508i</td>
</tr>
<tr>
<td>-26.935 - 376.49i</td>
<td>-13.371</td>
</tr>
<tr>
<td>-26.245 + 39.868i</td>
<td>-0.4248 + 0.8616i</td>
</tr>
<tr>
<td>-26.245 - 39.868i</td>
<td>-0.4248 - 0.8616i</td>
</tr>
<tr>
<td>-38.227</td>
<td></td>
</tr>
<tr>
<td>-3.5219 + 15.251i</td>
<td></td>
</tr>
<tr>
<td>-3.5219 - 15.251i</td>
<td></td>
</tr>
<tr>
<td>-13.371</td>
<td></td>
</tr>
<tr>
<td>-4.1084</td>
<td></td>
</tr>
<tr>
<td>-0.42476 + 0.86163i</td>
<td></td>
</tr>
<tr>
<td>-0.42476 - 0.86163i</td>
<td></td>
</tr>
<tr>
<td>-0.97768</td>
<td></td>
</tr>
</tbody>
</table>

From the digital simulation results shown in Fig. 4 it can be seen that the 5\(^{th}\) order model give a good accuracies. The optimal controller is designed in section 3, the feedback matrix is calculated by using Eq. (10) at nominal operating point (P=0.75 pu Q=0.0pu) to minimize the performance index J in Eq. (8)

\[
K_r = [-1.2584 \ 0.5948 \ -0.6375 \ -8.2231 \ -10.9569]
\]

Using this matrix the closed loop eigenvalues of system with optimal controller are calculated at different operating conditions and the results are tabulated in table 2.

The proposed ANN controller is constructed from two neural networks, this is discussed in section (5). The ANN1 is trained using input/output pairs of data which are collected from the optimal control of the reduced order model of power system at different loading conditions. The training data was fed to Matlab Tool Box to calculate the weights and biases of ANN1.
The statistical data for ANN1 training
No of iteration = 10000
Max. squared error = 1E-3
Learning rate = .001
The resulting weight matrix between the hidden and input neurons, and also the hidden nodes biases matrix are given by

\[ b_{11} = \begin{bmatrix}
-2.1918 \\
-2.3053 \\
-7.2796 \\
7.22 \\
23.759 \\
23.532 \\
77.5 \\
1.2978 \\
1.5152 \\
\end{bmatrix} \quad w_{11} = \begin{bmatrix}
1.9432 & 0.091295 \\
2.0553 & -0.0047312 \\
1.9152 & -12.154 \\
-1.8667 & 12.126 \\
-74.947 & 30.473 \\
-74.367 & 30.127 \\
-1.1156 & 128.77 \\
3.2499 & 1.9344 \\
-1.2181 & 1.7187 \\
\end{bmatrix} \]

The resulting weight matrix between the output and hidden neurons, and also the output nodes biases matrix are given by

\[ w_{21} = \begin{bmatrix}
-14.991 & 1.969 & 1.7769 & -7.8039 & -22.269 \\
13.698 & -1.7419 & -1.6922 & 9.1325 & 20.749 \\
-84.972 & -8.1071 & -0.50802 & 69.043 & 47.282 \\
-85.607 & -8.2762 & -0.5069 & 68.909 & 47.566 \\
-5.2901 & 3.2394 & 0.92924 & -9.5876 & 56.63 \\
5.7097 & -3.2119 & -0.75665 & 9.898 & -56.783 \\
8.0854 & 0.54458 & .0014447 & -8.9805 & 0.87331 \\
4.1223 & 0.36252 & 0.29057 & -0.74039 & -2.8098 \\
-4.1207 & 0.068004 & -0.11298 & 1.423 & 2.5943 \\
\end{bmatrix} \quad b_{21} = \begin{bmatrix}
-9.3186 \\
-0.49551 \\
-0.71995 \\
8.9751 \\
-4.725 \\
\end{bmatrix} \]

The ANN2 parameters are adapted on-line through the ANN1 according to loading conditions. The closed loop eigenvalues of system with proposed ANN controller are calculated at different operating condition by using Eq.18. The results of system with proposed ANN, with optimal controller and without controller are tabulated in Table 2.

To validate the above results, time responses of speed deviation for 0.01 pu increase in load power are drawn at a wide range of operating conditions. In each case the responses of the system with optimal controller and without controller are also given. Figures 5, 6, 7 and 9 show the rotor speed deviation response due to 0.01 load disturbance at large power factor loads at different controller. Figures 8 and 10 show the rotor speed deviation response due to 0.01 load disturbance at lead power factor loads at different controller.
It can be concluded from these results that the system with optimal controller give good dynamic response and the system with proposed ANN give responses better than the responses of the system with optimal controller. Figures 8, 10 and 11 show the system without controller and with optimal controller suffers from synchronous instability in other hand the system with proposed ANN controller provide good dynamic response at the same operating conditions. The comparison of settling time between different controllers are given in table 3.

Table 2: Eigenvalue at different controller and at different operating conditions of the reduced order model.

<table>
<thead>
<tr>
<th>Load condition</th>
<th>System without controller</th>
<th>System with optimal controller</th>
<th>System with proposed ANN controller</th>
</tr>
</thead>
<tbody>
<tr>
<td>P=0.75 Q=0.0</td>
<td>-3.5219 +15.2508i</td>
<td>-9.6721 +15.2263i</td>
<td>-10.4165 +15.3774i</td>
</tr>
<tr>
<td></td>
<td>-13.3713</td>
<td>-0.3119</td>
<td>-0.6208</td>
</tr>
<tr>
<td></td>
<td>-0.4248 + 0.8616i</td>
<td>-11.7442 + 0.5954i</td>
<td>-7.7532</td>
</tr>
<tr>
<td></td>
<td>-0.4248 - 0.8616i</td>
<td>-11.7442 - 0.5954i</td>
<td>-17.4330</td>
</tr>
<tr>
<td>P=0.25 Q=0.0</td>
<td>-6.4568 + 18.531i</td>
<td>-6.4568 + 18.531i</td>
<td>-9.4082 + 18.28i</td>
</tr>
<tr>
<td></td>
<td>-6.4568 - 18.531i</td>
<td>-6.4568 - 18.531i</td>
<td>-9.4082 - 18.28i</td>
</tr>
<tr>
<td></td>
<td>-7.1595</td>
<td>-7.1595</td>
<td>-1.2219</td>
</tr>
<tr>
<td></td>
<td>-0.5578 + 0.3351i</td>
<td>-0.5578 + 0.3351i</td>
<td>-6.0768</td>
</tr>
<tr>
<td></td>
<td>-0.5578 - 0.3351i</td>
<td>-0.5578 - 0.3351i</td>
<td>-17.095</td>
</tr>
<tr>
<td>P=0.75 Q=0.6</td>
<td>-14.6084</td>
<td>-4.2354 +10.7103i</td>
<td>-1.2264</td>
</tr>
<tr>
<td></td>
<td>-2.6732 +13.2562i</td>
<td>-4.2354 -10.7103i</td>
<td>-6.2935 +10.8393i</td>
</tr>
<tr>
<td></td>
<td>-2.6732 -13.2562i</td>
<td>-1.1834</td>
<td>-6.2935 -10.8393i</td>
</tr>
<tr>
<td></td>
<td>-0.5075 + 0.4225i</td>
<td>-16.8061 + 7.3942i</td>
<td>-15.9735 + 4.3691i</td>
</tr>
<tr>
<td></td>
<td>-0.5075 - 0.4225i</td>
<td>-16.8061 - 7.3942i</td>
<td>-15.9735 - 4.3691i</td>
</tr>
<tr>
<td>P=0.75 Q=-0.6</td>
<td>-19.5200</td>
<td>0.2414</td>
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<td>0.2410 +12.2945i</td>
<td>-3.8598 +10.8910i</td>
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<td>-18.3961 + 8.6234i</td>
<td>-0.8057</td>
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<td>-0.4137 +12.4600i</td>
<td>-18.3961 - 8.6234i</td>
<td>-6.5433 + 9.5543i</td>
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<td>-2.6355 + 9.6792i</td>
<td>-6.5433 - 9.5543i</td>
</tr>
<tr>
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<td>-0.4443 + 0.7734i</td>
<td>-2.6355 - 9.6792i</td>
<td>-16.7937 + 4.2975i</td>
</tr>
<tr>
<td></td>
<td>-0.4443 - 0.7734i</td>
<td>-0.6384</td>
<td>-16.7937 - 4.2975i</td>
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<tr>
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<td>-27.4922</td>
<td>-24.7373</td>
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<tr>
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<td>0.6424 +11.9901i</td>
<td>-3.0553 +10.5244i</td>
<td>-7.3560 +10.4867i</td>
</tr>
<tr>
<td></td>
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<td>-3.0553 -10.5244i</td>
<td>-7.3560 -10.4867i</td>
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<td>-0.7657</td>
<td>-11.2971</td>
<td>-13.9946</td>
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Fig. 4: Rotor speed deviation response due to 0.01 pu load disturbance for original and reduced order model at loading condition ($P = 0.75 \ Q = 0.0$).

Fig. 5: Rotor speed deviation response due to 0.01 pu load disturbance at loading condition ($P = 0.25 \ Q = 0.0$).
Fig. 6: Rotor speed deviation response due to 0.01 pu load disturbance at loading condition (P = 0.75 Q = 0.0).

Fig. 7: Rotor speed deviation response due to 0.01 pu load disturbance at loading condition (P = 0.75 Q = 0.6).
Fig. 8: Rotor speed deviation response due to 0.01 pu load disturbance at different controller at loading condition ($P = 0.75$, $Q = -0.6$).

Fig. 9: Rotor speed deviation response due to 0.01 pu load disturbance at loading condition ($P = 1.2$, $Q = 0.6$).
Fig. 10: Rotor speed deviation response due to 0.01 pu load disturbance at loading condition (P=1.2 Q=-0.6).

Fig. 11: Rotor speed deviation response due to 0.01 pu load disturbance at loading condition (P=1.2 Q=-0.6).
Table 3: Settling time of different cases at different loading condition.

<table>
<thead>
<tr>
<th>Loading condition</th>
<th>Without controller</th>
<th>With optimal controller</th>
<th>With proposed ANN controller</th>
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<tbody>
<tr>
<td>P=0.25 Q=0.0</td>
<td>6 Sec.</td>
<td>1.5 Sec.</td>
<td>1.2 Sec.</td>
</tr>
<tr>
<td>P=0.75 Q=0.6</td>
<td>7 Sec.</td>
<td>3 Sec.</td>
<td>∞ Sec.</td>
</tr>
<tr>
<td>P=0.75 Q=-0.6</td>
<td>∞ Sec.</td>
<td>∞ Sec.</td>
<td>3.5 Sec.</td>
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</tbody>
</table>

7. CONCLUSION

An optimal artificial neural network controller has been developed to be included in power systems in order to improve the dynamic response of this system and to give an optimal performance at any loading condition. The proposed controller has ability to adapt its parameters at any loading condition. This controller is designed based on reduced order model of power system in order to retain only the states, which are measurable or observable. The feature of this controller is the reduction of the consuming time and reduction of the number of neurons, which are required for proposed ANN structure. The obtained results show the effectiveness of proposed ANN controller in enhancing the damping characteristic of the studied power system at any loading condition in comparison with optimal feedback controllers. The proposed controller has better performance than the optimal feedback controller in terms of fast damping response and small settling time.

8. REFERENCES

APPENDICES

Appendix-a: Elements definition of A-matrix

\[ \psi_{d0} = -x_d I_{d0} + x_{md} I_{f0} \]

\[ \psi_{q0} = x_q I_{q0} \]

\[ M10.1 = \frac{K_r V_{q0} r_i - K_r V_{d0} x_i}{T_r V_{i0}} \]

\[ M10.2 = \frac{K_r V_{q0} x_j - K_r V_{d0} r_i}{T_r V_{r0}} \]

\[ M10.6 = \frac{K_r V_{q0} V_b \sin \delta_0 + K_r V_{d0} V_b \cos \delta_0}{T_r V_{r0}} \]

\[ M10.7 = \frac{K_r V_{q0} I_{d0} x_j - K_r V_{d0} I_{q0} x_j}{T_r V_{r0}} \]

\[ \psi_{d0} = -x_d I_{d0} + x_{md} I_{f0} \]

\[ \psi_{q0} = x_q I_{q0} \]

\[ M10.1 = \frac{K_r V_{q0} r_i - K_r V_{d0} x_i}{T_r V_{i0}} \]

\[ M10.2 = \frac{K_r V_{q0} x_j - K_r V_{d0} r_i}{T_r V_{r0}} \]

\[ M10.6 = \frac{K_r V_{q0} V_b \sin \delta_0 + K_r V_{d0} V_b \cos \delta_0}{T_r V_{r0}} \]

\[ M10.7 = \frac{K_r V_{q0} I_{d0} x_j - K_r V_{d0} I_{q0} x_j}{T_r V_{r0}} \]
Appendix-b :System parameters

Table b-1: parameter of one machine -infinite bus( in per unit).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
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<tr>
<td>$X_d$</td>
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<tr>
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<tr>
<td>$V_b$</td>
<td>1</td>
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</table>

稳定性电网的参数

为了评估网格的稳定性，我们根据不同的运行条件和网络结构调整控制参数，以便在不同的运行条件下实现最优性能。通过对实际运行数据的分析，我们发现在原网络自适应控制器的基础上，提出了一种改进的控制器，该改进控制器在一定程度上改善了系统的动态性能。