



الامتحان مكون من أربع صفحات، الإجابة في نفس ورقة الأسئلة.
حاول في كل الأسئلة، النهاية العظمى ٤٠ درجة.
الإجابة النهائية يجب أن تكون مكتوبة في المكان المخصص لها.

Question # 1: (4 Points)

Consider the design of a circuit to subtract two binary bits, yielding a one-bit difference and a one-bit borrow. Four cases can arise:

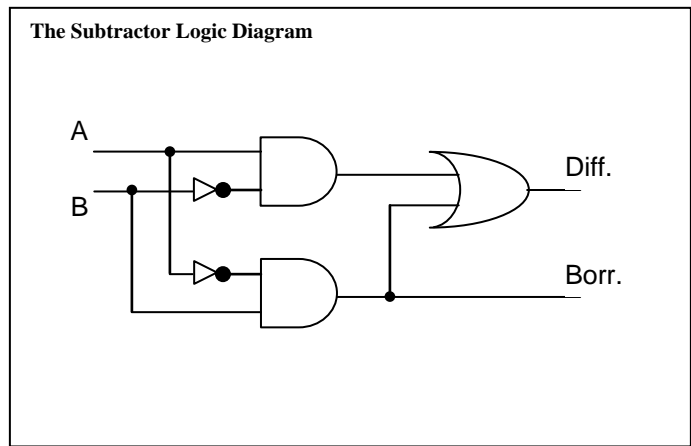
0 from 0 result is 0 borrow 0, 0 from 1 result is 1 borrow 0, 1 from 0 result is 1 borrow 1, and 1 from 1 result is 0 borrow 0.

Using simple logic gates (AND, OR, Inverter) design a circuit that behaves in this way.

Dec.	Input		Output	
	A	B	Diff.	Borr.
0	0	0	0	0
1	0	1	1	1
2	1	0	1	0
3	1	1	0	0

$$\text{Diff.} = A \cdot B' + A' \cdot B$$

$$\text{Borr.} = A' \cdot B$$



Question # 2: (3 Points)

The state of a 12-bit register is 100101010100. What is its content if it represents:

- (a) Three decimal digits in BCD,
- (b) Three decimal digits in the excess-3 code,
- (c) Three decimal digits in the 84-2-1 code?

BCD: 954

excess-3: 621

84-2-1: 734

Question # 3: (4 Points)

Using DeMorgan's theorem find the complement of the following expressions:

$$F_1 = x' y' + x' z + y' z$$

$$F_2 = (A'B + CD)E + E'$$

$$F_1' = (x + y)(x + z)(y + z)$$

$$= xy + xz + yz'$$

$$F_2' = ((A + B')(C' + D) + E') \cdot E$$

$$= AC'E + ADE + B'C'E + B'DE$$

Question # 4: (4 Points)

A combinational circuit is defined by the following two Boolean functions:

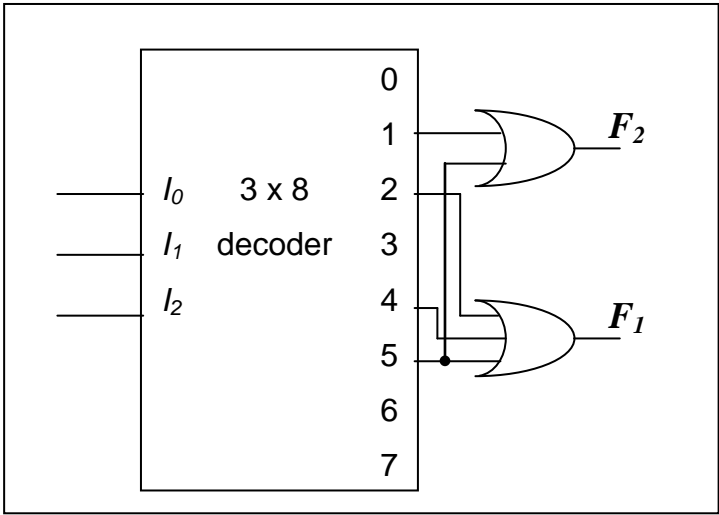
$$F_1(x, y, z) = x'y z' + xy'$$

$$F_2(x, y, z) = y'z (x'z + xy')$$

Find the min-terms of the functions, and implement them with a single decoder and external gates.

$$F_1(x, y, z) = \Sigma m(2, 4, 5)$$

$$F_2(x, y, z) = \Sigma m(1, 5)$$



Question # 5: (4 Points)

Derive the state table and the state diagram of the sequential circuit shown in Fig.5.

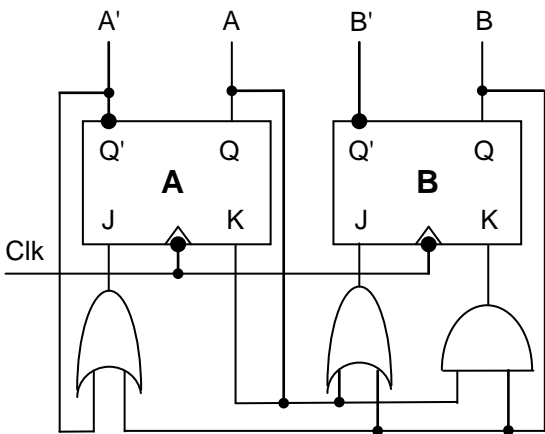
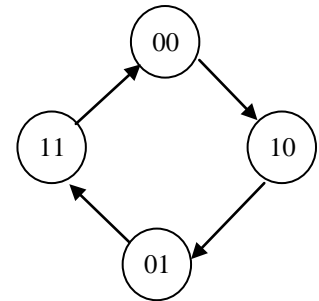


Fig.5

Present State		F.F. Inputs				Next State	
A	B	JA	KA	JB	KB	A	B
0	0	1	0	0	0	1	0
0	1	1	0	1	0	1	1
1	0	0	1	1	0	0	1
1	1	1	1	1	1	0	0



Question # 6: (3 Points)

Specify the number of address lines, data lines and the capacity in kilo-bytes of a 65536x32 RAM.

Address lines = 16 Lines

Data lines = 32 Lines

Capacity in Kbytes = 256 KB

Question # 7: (4 Points)

Show the main difference between latches and flip-flops by drawing the timing diagram of the output Q when applying the clk and input D shown in Fig. 7 to:

- i) A positive level-triggered latch,
- ii) A negative edge-triggered flip-flop.

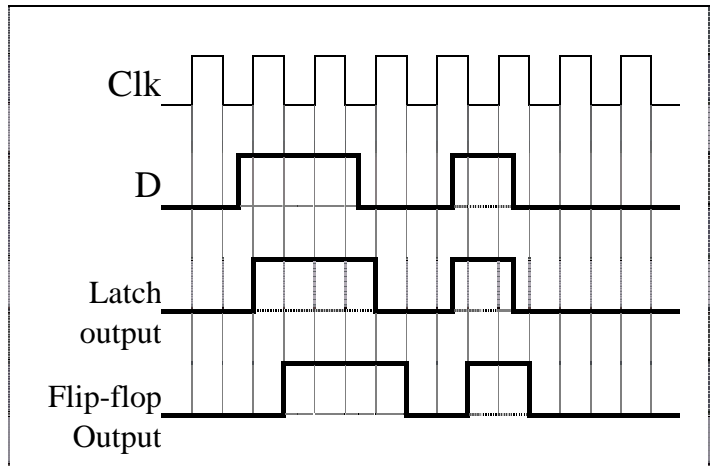


Fig. 7

Question # 8: (6 Points)

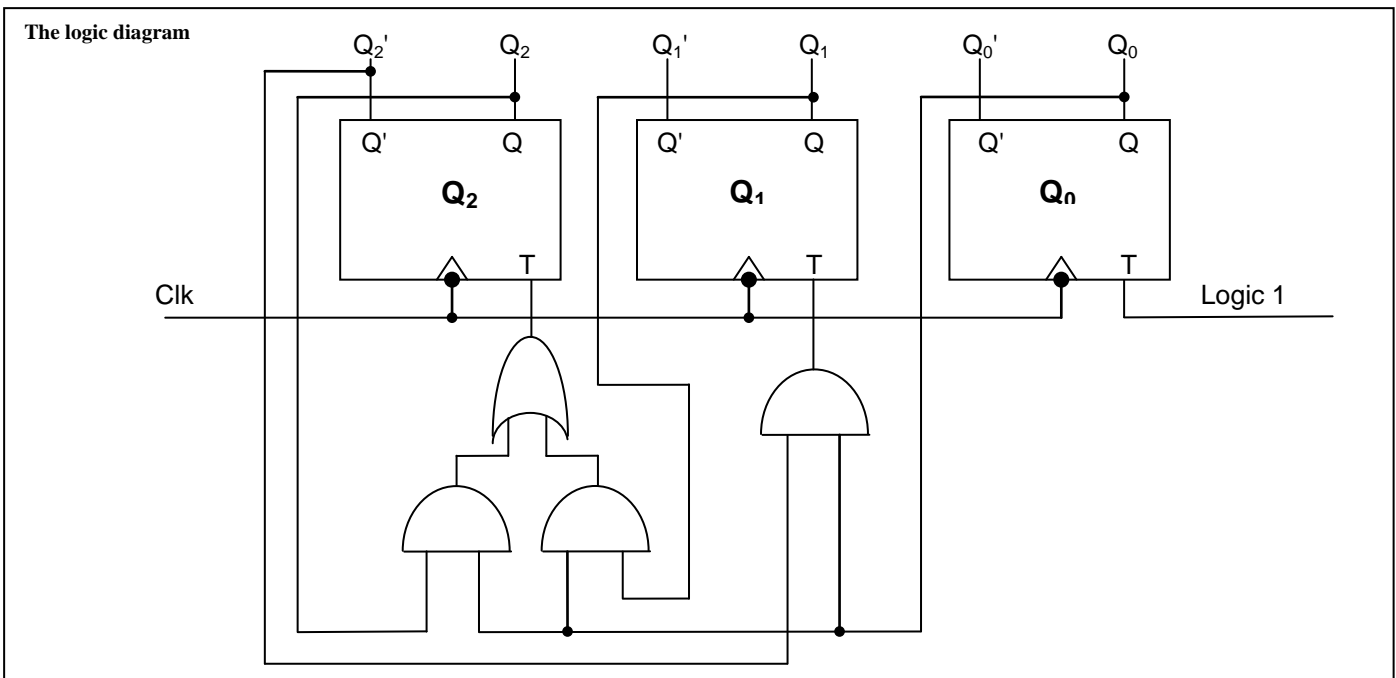
Design a synchronous mod-6 counter (counts 0-5) using T flip-flops and logic circuitry. Consider the unused states as don't care.

Present State			Next State			Flip-Flop Inputs		
Q2	Q1	Q0	Q2	Q1	Q0	T2	T1	T0
0	0	0	0	0	1	0	0	1
0	0	1	0	1	0	0	1	1
0	1	0	0	1	1	0	0	1
0	1	1	1	0	0	1	1	1
1	0	0	1	0	1	0	0	1
1	0	1	0	0	0	1	0	1
1	1	0	x	x	x	x	x	x
1	1	1	x	x	x	x	x	x

$T_0 = 1$

$T_1 = Q_2' Q_0$

$T_2 = Q_2 Q_0 + Q_1 Q_0$



Question # 9: (8 Points)

List the PLA programming table that implements the following Boolean functions using the minimum number of product terms:

$$F1(A, B, C, D) = \Sigma m(1, 3, 5, 7, 10, 11)$$

$$F2(A, B, C, D) = \Sigma m(1, 2, 5, 6, 8, 9, 10, 11)$$

$$F3(A, B, C, D) = \Sigma m(0, 4, 10, 11, 12, 13, 14, 15)$$

CD AB	00	01	11	10
00		1	1	
01		1	1	
11		1	2	
10			3	1

PLA Programming Table

Product Term	Inputs				Outputs		
	A	B	C	D	(T)	(T)	(C)
	F1	F2	F3				
1: A'C'D	0	-	0	1	1	1	1
2: A'CD	0	-	1	1	1	-	1
3: AB'C	1	0	1	-	1	1	-
4: A'CD'	0	-	1	0	-	1	1
5: AB'C'	1	0	0	-	-	1	1

CD AB	00	01	11	10
00		1		1
01		1		1
11		1		4
10	1	5	1	3

$$F1 = A'C'D + A'CD + AB'C$$

$$F2 = A'C'D + AB'C + A'CD' + AB'C'$$

$$F3' = A'C'D + A'CD + A'CD' + AB'C'$$

CD AB	00	01	11	10
00		0	0	0
01		0	0	0
11		1	2	4
10	0	5		

**** Best Wishes ****

Prof. Magdy M. Doss